

**Exam Electronics & Signal processing**  
**PHYSICS - Students**  
**11 April, 2012**  
**Dr. G. Palasantzas**

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## Problem 1

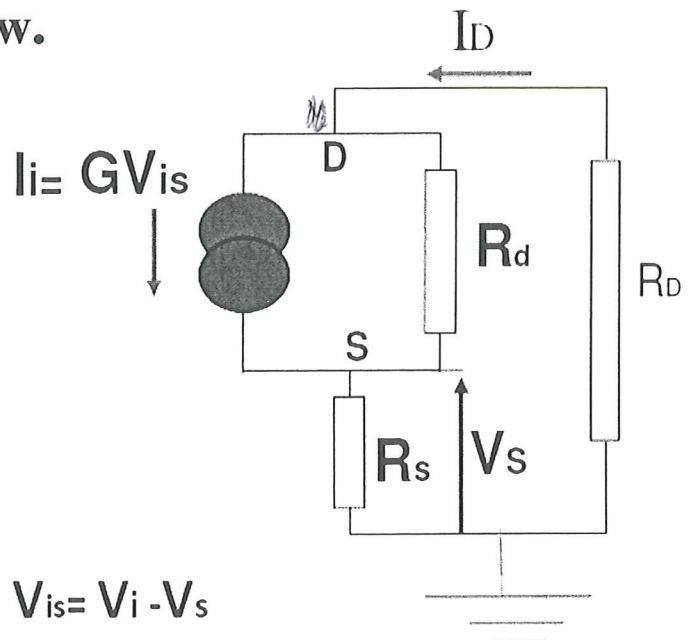
(1.5 point)

Assume that an external voltage  $V_i$  drives a circuit in a way that we can represent its effect via a current source  $I_i = G V_{is} = G(V_i - V_s)$  in parallel with a resistor  $R_d$  as shown below.

$G$ : is a constant

$V_D$ : Potential at point D

$V_s$ : potential at point S



Then prove for  $V_s/V_i$ :

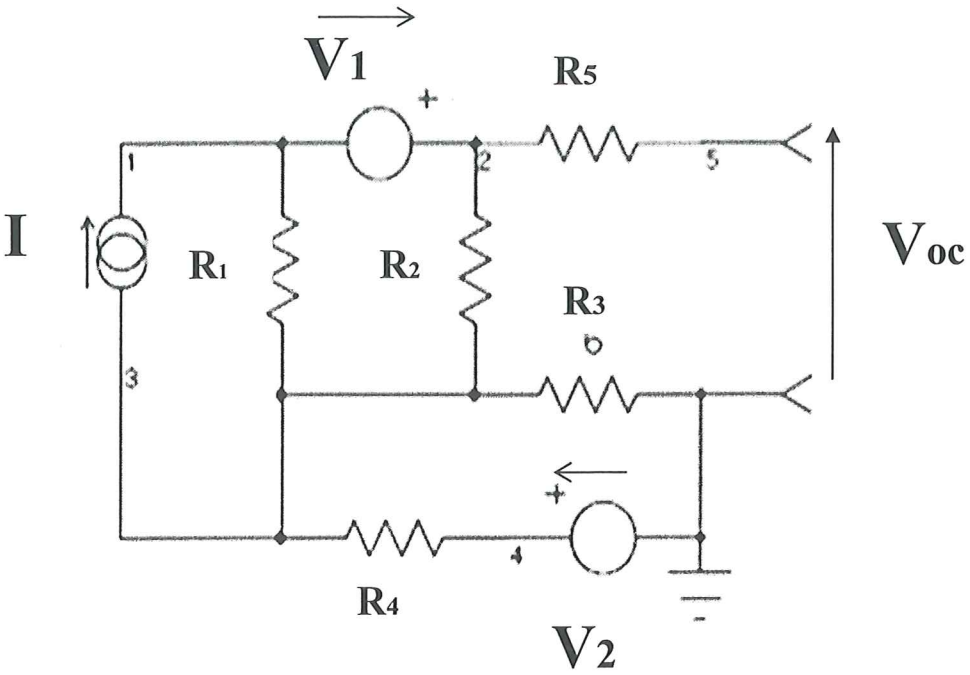
$$V_s / V_i = G R_s / [ 1 + G R_s + [(R_s + R_D) / R_d] ]$$

$$\frac{V_s}{V_i} = \frac{G R_s}{1 + G R_s + \frac{R_s + R_D}{R_d}}$$

# Problem 2

(1.5 points)

Consider the Circuit →

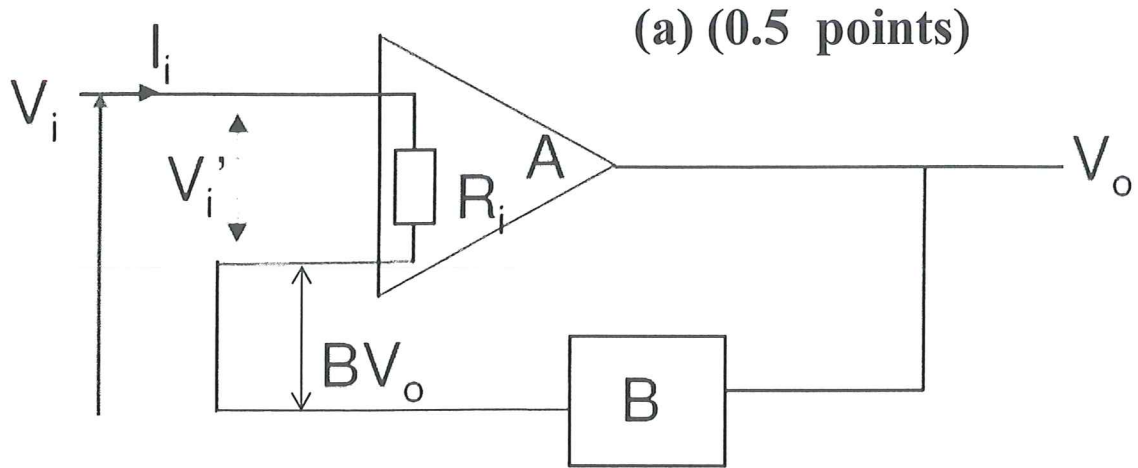


Give the equivalent Thévenin and calculate  $V_{oc}$  en  $R_{oc}$ .

↑

v

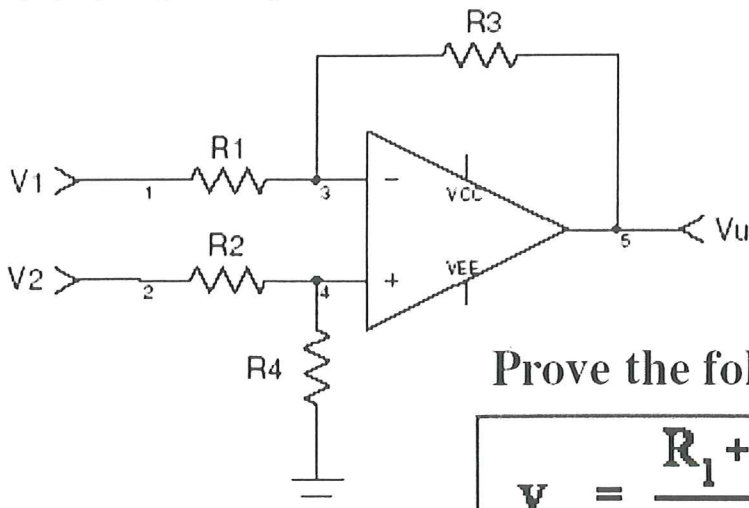
### Problem 3



Prove that the feedback increases the input resistance  $R_i$  of an amplifier or:

Input resistance  $= \frac{V_i}{I_i} = R_i(1 + AB)$

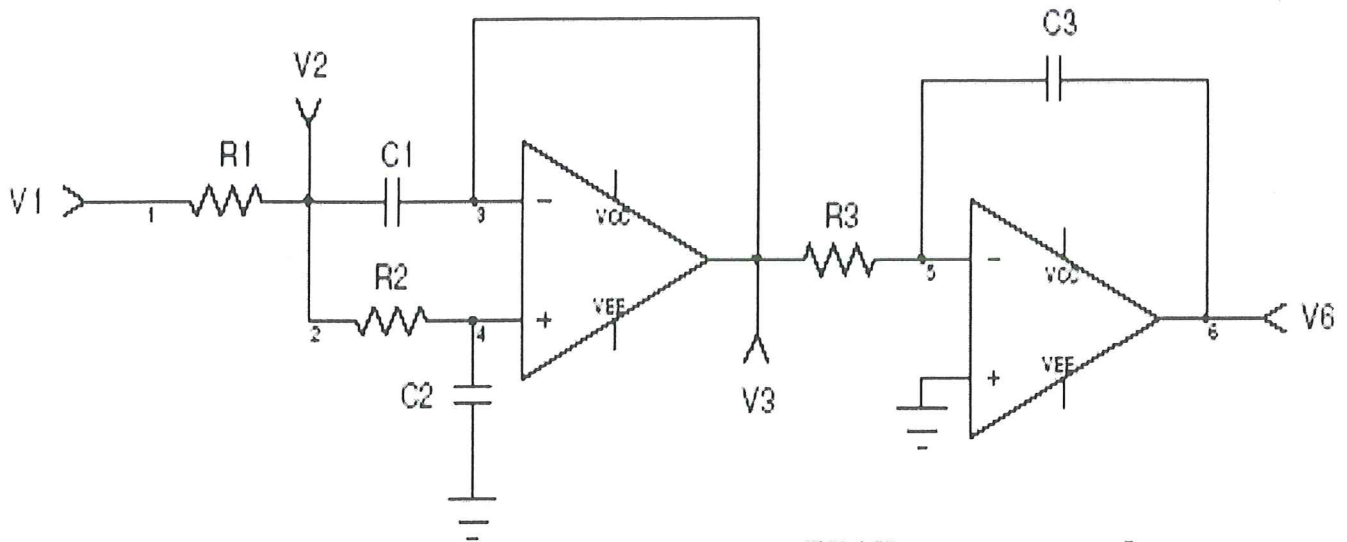
(b) (1 point)



Prove the following:

$$V_u = \frac{R_1 + R_3}{R_2 + R_4} \frac{R_4}{R_1} V_2 - \frac{R_3}{R_1} V_1$$

## Problem 4



(a: 0.5 points) Prove:

$$\frac{V(6)}{V(3)} = - \frac{1}{j\omega\tau_3}$$

$$\tau_3 = R_3 C_3$$

(b: 1 point) Prove:

$$V(2) = \frac{\left(\frac{R_1}{R_2} + j\omega\tau_1\right) V(3) + V(1)}{1 + \frac{R_1}{R_2} + j\omega\tau_1}$$

$$\tau_1 = R_1 C_1$$

(c: 0.5 points) Prove:  $V(3) = V(4) = \frac{V(2)}{1 + j\omega\tau_2}$

$$\tau_2 = R_2 C_2$$

**Tips:** Ideal opamps ( $V^+ = V^-$ ). For (b) use superposition between  $V(3)$  and  $V(1)$  and  $V(3) = V(4)$  [if you do this correctly then you have done the most essential step for (b)].

## Problem 5

(a: 0.5 points)

		AB			
		00	01	11	10
CD	00	1	0	0	0
	01	1	1	1	0
	11	1	1	0	1
	10	1	0	0	0

Prove:

$$Y = \overline{A}\overline{B} + \overline{A}D + B\overline{C}D + \overline{B}CD$$

(b: 0.5 points)

		AB			
		00	01	11	10
CD	00	0	0	x	0
	01	1	1	x	1
	11	0	0	x	x
	10	1	1	x	x

Prove:

$$Y = C\overline{D} + \overline{C}D$$

x: don't care

Tip: indicate the proper grouping of terms

**(c) (1.5 points)**

**Build a synchronous 3-counter (1→4) / use 3 J-K**

Voor			Na			
	Q3	Q2	Q1	Q3	Q2	Q1
1	0	0	1			
2	0	1	0			
3	0	1	1			
4	1	0	0			

$Q_{n-1}$	$Q_n$	J	K
0	0	0	*
0	1	1	*
1	0	*	1
1	1	*	0

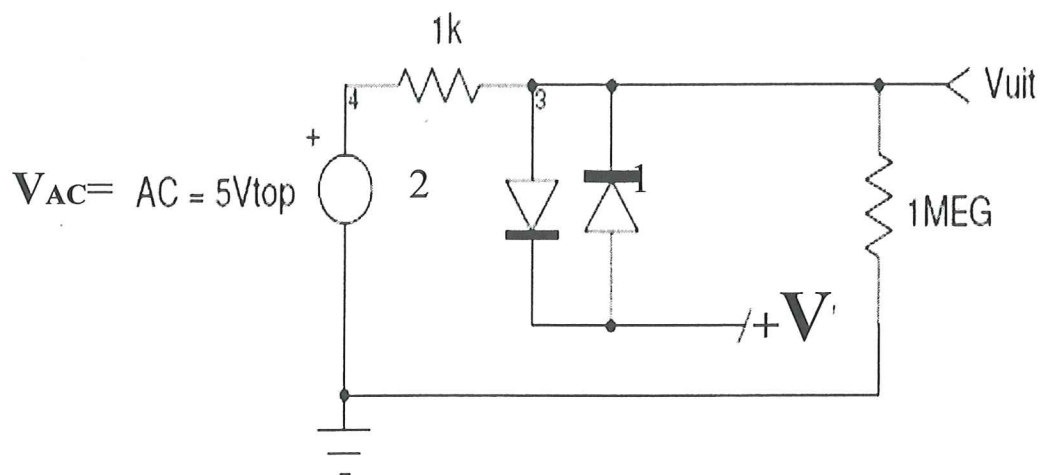
**\*: don't care**

J	K	$Q_n$
0	0	$Q_{n-1}$
0	1	0
1	0	1
1	1	$\overline{Q_{n-1}}$

## Problem 6

(1 point)

Assume that  $V + V_c < V_{AC}$



$V_c = 0.5 \text{ V}$  (diode voltage for forward conduction)  
 $V = 3.5 \text{ V}$

Draw  $V_{uit}$

DONNERDAG NA 15:00

VRJ DAG VOOR 15:00



## Boolean laws:

$$\overline{A+B} = \overline{A} \cdot \overline{B}$$

$$\overline{A \cdot B} = \overline{A} + \overline{B}$$

$$A + AB = A$$

$$A(A+B) = A$$








$$(AB)C = A(BC)$$

$$(A+B)+C = A+(B+C)$$

$$A(B+C) = AB+AC$$

$$(A+B)(A+C) = A+BC$$

Tabel 1 Logische poorten.

Functie	Symbol	Boolean	Waarheidstabel															
AND		$C = A \cdot B$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td><td>C</td></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table>	A	B	C	0	0	0	0	1	0	1	0	0	1	1	1
A	B	C																
0	0	0																
0	1	0																
1	0	0																
1	1	1																
OR		$C = A + B$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td><td>C</td></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table>	A	B	C	0	0	0	0	1	1	1	0	1	1	1	1
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1	0	1																
1	1	1																
NOT		$B = \overline{A}$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td></tr> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </table>	A	B	0	1	1	0									
A	B																	
0	1																	
1	0																	
NAND		$C = \overline{A \cdot B}$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td><td>C</td></tr> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> </table>	A	B	C	0	0	1	0	1	1	1	0	1			
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0	0	1																
0	1	1																
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NOR		$C = \overline{A + B}$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td><td>C</td></tr> <tr><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </table>	A	B	C	0	0	1	0	1	0	1	0	0	1	1	0
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XOR		$C = A \oplus B$	<table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td>A</td><td>B</td><td>C</td></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>0</td></tr> </table>	A	B	C	0	0	0	0	1	1	1	0	1	1	1	0
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